## WORKSHEET: §2.3

- 1. Fill in the blanks below. Assume a and c are fixed constants. (Note that these are all in your text but not in this order.) Assume  $\lim_{x \to a} f(x)$  and  $\lim_{x \to a} g(x)$  exist.
  - (a)  $\lim_{x \to a} c =$  \_\_\_\_\_
  - (b)  $\lim_{x \to a} x =$  \_\_\_\_\_
  - (c)  $\lim_{x \to a} (f(x) + g(x)) =$ \_\_\_\_\_
    - i. What do the rules above imply about  $\lim_{x \to 12} (x + \pi)$ ?

(d)  $\lim_{x \to a} (f(x) - g(x)) =$ \_\_\_\_\_

- (e)  $\lim_{x \to a} cf(x) =$  \_\_\_\_\_
  - i. What do the rules above imply about  $\lim_{x\to 5} 2x + 3$ ?
- (f)  $\lim_{x \to a} f(x)g(x) =$ \_\_\_\_\_
- (g)  $\lim_{x \to a} x^n =$ \_\_\_\_\_
- (h)  $\lim_{x \to a} (f(x))^n =$ \_\_\_\_\_
- (i)  $\lim_{x \to a} \frac{f(x)}{g(x)} =$ \_\_\_\_\_ provided \_\_\_\_\_
- (j)  $\lim_{x \to a} \sqrt[n]{x} =$
- (k)  $\lim_{x \to a} \sqrt[n]{f(x)} =$ \_\_\_\_\_

2. If 
$$\lim_{x \to \sqrt{2}} f(x) = 8$$
 and  $\lim_{x \to \sqrt{2}} g(x) = e^2$ , then evaluate

$$\lim_{x \to \sqrt{2}} \left( \frac{g(x)}{(3 - f(x))^2} + 2\sqrt{g(x)} \right)$$

3. Use the previous rules to evaluate (a) and explain why you *cannot* use the rules to evaluate (b).

(a) 
$$\lim_{w \to -\frac{1}{2}} \frac{2w+1}{w^3}$$

(b) 
$$\lim_{t \to 1} \frac{t^2 + t - 2}{t^2 - 1}$$

4. (One more super-useful rule!) If

, then  $\lim_{x \to a} f(x) = \lim_{x \to a} g(x)$ 

5. Use this rule and what you know about zeros of polynomials to evaluate

$$\lim_{t \to 1} \frac{t^2 + t - 2}{t^2 - 1}$$

UAF Calculus 1