

SECTION 3-4: DERIVATIVES AS RATES OF CHANGE

Read Section 3.4. Work the embedded problems.

1. A potato is launched vertically upward from a platform 20 feet off the ground. The distance in feet that the potato travels from the ground after  $t$  seconds is given by  $s(t) = -16t^2 + 64t + 20$ .

(a) Find the initial velocity of the potato.

$$v(t) = s'(t) = -32t + 64;$$

Initial velocity is when  $t=0$ :

$$v(0) = 64 \text{ ft/sec}$$

(b) Find the velocity and the acceleration of the potato when  $t = 3$ .

$$\begin{array}{r} 32 \\ -96 \\ +64 \\ \hline -32 \end{array}$$

$$v(3) = -32(3) + 64 = -32 \text{ ft/sec}$$

$$a(t) = -32 \text{ ft/sec}^2$$

(c) Is the potato speeding up or slowing down? Why?

The potato is speeding up because  $a(3)$  and  $v(3)$  are both the same sign (ie negative)

(d) What is the velocity of the potato when it reaches its maximum height and why?

At maximum height  $v(t) = 0$  because the potato stops going up (pos. vel) and starts going down (neg. vel). So it's zero.

(e) What is the maximum height of the potato?

Set  $v=0$  to find  $t$ :  $0 = -32t + 64$ . So  $t=2$ .

$$s(2) = -16 \cdot 4 + 64 \cdot 2 + 20 = 84 \text{ ft.}$$

(f) Assume the potato lands on the ground (not the platform). How long is the potato in the air?

Find  $t$  when  $s=0$ .

$$0 = -16t^2 + 64t + 20$$

$$t = \frac{-64 \pm \sqrt{64^2 - 4(-16)(20)}}{2(-16)} \approx 4.29135$$

Ignore the negative root!

(g) What is the velocity of the potato when it hits the ground?

$$v(4.2913) = -32(4.2913) + 64 = -73.32 \text{ ft/s}$$

(h) You should have observed in part (b) that the acceleration is constant. What does this number represent?

It is the acceleration due to gravity on earth.

$$\begin{array}{r} 2 \\ 16 \\ \hline 64 \\ 128 \\ \hline 148 \\ -64 \\ \hline 84 \end{array}$$