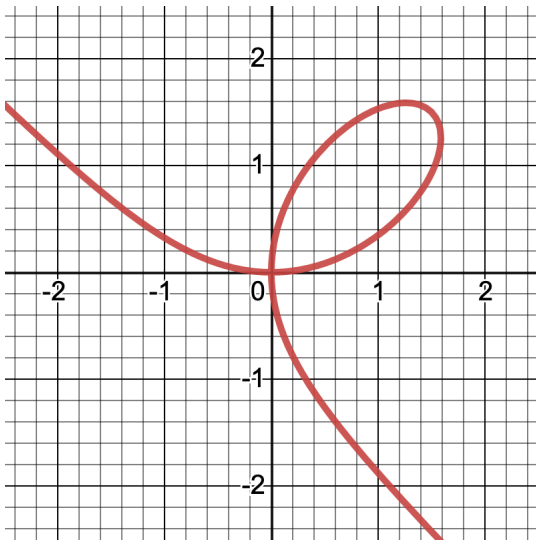


SECTION 3-8: IMPLICIT DIFFERENTIATION

1. Motivating questions: How can we find slope of the tangent / velocity for a graph that looks like the one below?



Tangent line to $y^3 + x^3 = 3xy$ at $(3/2, 3/2)$?

2. What is the derivative of: $(f(x))^3$?
3. Repeat question 2 above but with Leibniz notation. What is dy/dx for: $(y)^3$?
4. What is the derivative of $3xg(x)$?
5. Repeat question 4 above but with Leibniz notation. What is dy/dx for: $3xy$?

6. Find dy/dx for each expression below.

(a) $y \cos(x) + 2x = (y + 1)^2$

(b) $x + \tan(xy) = 5$

7. For the equation $x^2 + xy + y^2 = 9$,

(a) find the x intercept(s)

(b) Find the slope of the tangent lines at the x -intercepts.

(c) Write the equations of the tangent lines at the x -intercepts.

(d) Sketch a picture of the curve and its tangent lines from part (c)