

THE END OF CHAPTER 3 AND THE START OF CHAPTER 4

1. (A quick refresher from Monday.) Find the derivatives of the functions below.

(a) $y = e^{2x} + \ln(2x)$

(b) $y = e^2 + e^{\sin(cx)}$ where c is a constant.

(c) $y = x^3 \sin(10^x)$

(d) $w(r) = \ln(\tan^{-1}(r))$

(e) $f(x) = x^{\ln(x)}$ Hint: Use logarithmic differentiation (which means to start by taking the natural log of both sides of the equation.)

2. For each of the functions: $f(x) = P_0 e^{kt}$, $f(x) = x^2$ and $f(x) = x^{10}$ write $f'(x)$ in terms of $f(x)$. Can you tell what $f^{(50)}$ is?

3. Chapter 4 is about applications of the derivative. Section 4.1 is about Related Rate Problems.

Example: A 15-ft ladder is leaning against a wall. The top of the ladder slides down the wall. Assume that the ladder is rigid and does not shorten or lengthen as it slides. Draw a picture. Label with variables the lengths that are changing over time. Label with constants the things that are fixed. Which variables do you expect to have a positive derivative with respect to time? Negative? Zero? What equations can you think of that related some of the variables in your picture?

4. A list of derivative rules you will need to *know* how and when to use.

(a) $\frac{d}{dx} [f(x)g(x)] =$

(b) $\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] =$

(c) $\frac{d}{dx} [f(g(x))] =$

(d) $\frac{d}{dx} [\sin(x)] =$

(e) $\frac{d}{dx} [\cos(x)] =$

(f) $\frac{d}{dx} [\tan(x)] =$

(g) $\frac{d}{dx} [\sec(x)] =$

(h) $\frac{d}{dx} [\cot(x)] =$

(i) $\frac{d}{dx} [\csc(x)] =$

(j) $\frac{d}{dx} [\sin^{-1}(x)] =$

(k) $\frac{d}{dx} [\cos^{-1}(x)] =$

(l) $\frac{d}{dx} [\tan^{-1}(x)] =$

(m) $\frac{d}{dx} [e^x] =$

(n) $\frac{d}{dx} [a^x] =$

(o) $\frac{d}{dx} [\ln(x)] =$

(p) $\frac{d}{dx} [\log_a(x)] =$