1. Find the derivative of each of the following. Use whatever rule you choose. Simplify if you have time.

$$d' [x^{r} f(x) = 5e^{2} + 4x^{3/4} + 5x\sin(x)$$

$$f'(x) = 0 + 4f \cdot \frac{3}{4}x^{-1/4} + 5x(4x(x)) + 5 \cdot 1 \cdot 3in(x)$$

$$= 3x^{-1/4} + 5x\cos(x) + 5\sin(x)$$

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$$= 3x^{-1/4} + 5x\cos(x) + 5\sin(x)$$

$$= 2x^{-2} + \frac{1}{2} + \frac{(x+b)(-\sin(x)) - (a_{0}x)(1)}{(x+b)^{2}}$$

$$= \frac{2}{3} - 2x^{-1} + \frac{1}{2}x + \frac{\cos(x)}{x+b}$$

$$= 2x^{-2} + \frac{1}{2} + \frac{-((x+b)\sin(x) + \cos(x))}{(x+b)^{2}}$$

$$d' h(x) = \frac{1}{3x}(8 + x^{2}) = \frac{1}{3}x^{-1}(8 + x^{2})$$

$$= \frac{9}{3}x^{-1} + \frac{1}{3}x$$

$$H'(x) = -\frac{9}{3}x^{-2} + \frac{1}{3}$$

$$f'(x) = -\frac{9}{8x^{-2}} + \frac{1}{3}$$

$$f'(x) = -\frac{1}{8x^{-2}} - 8x^{-2} + 1$$

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Problems were reordered!

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2. Determine the point (or points) where the graph  $f(x) = x^3$  has a slope of 2.

$$f'(x) = 3x^{2}$$

$$m=2$$
So  $3x^{2}=2$  or
$$x = \pm\sqrt{\frac{2}{3}}$$

$$y = \sqrt{\frac{2}{3}}$$

- 3. An ant walking along a sidewalk has traveled  $s(t) = t^4 2t^2$  inches in *t* minutes. Find the acceleration of the ant (with units) when the velocity of the ant is 0.
- $S'(t) = V(t) = 4t^{3}-4t$   $S''(t) = V'(t) = a(t) = 12t^{2}-4$  *e-units inches/minute/minute = in/min<sup>2</sup>*  V=S'=0 when  $4t^{3}-4t = 4t(t^{2}-1) = 4t(t-1)(t+1) = 0$  or t=0, 1, -1. a(0) = -4, a(1) = 8, a(-1) = 8 all in  $in/min^{2}$ 
  - 4. The concentration of an antibiotic in the bloodstream *t* hours after being injected is given by  $C(t) = \frac{2t^2 + t}{t^3 + 50}$  where *C* is measured in milligrams per liter of blood.
    - (a) Find C(0) and C(10) and explain what these numbers mean in the context of the problem. Before, the injection, the concentration in the blood is

$$C(0) = 0$$

$$Eevo: Ten house after the injection, the concentration
$$C(10) = \frac{Z_{10}}{1050} = 0.20$$
in the blood is  $0.2 \text{ mg/L}$ .  
(b) It is a fact that  $C'(t) = \frac{-2(t^4+t^3-100t-25)}{(t^3+50)^2}$ . What are the units of  $C'(x)$ ?  
(milligrams per liter) per hour or  $mg/L/hr$$$

(c) It is a fact that C'(10) = -0.018. Interpret this fact in the context of the problem. Use language a Precalculus student could understand.
Ten hous after the injection, the concentration of antibiotic in the block is decleasing at a rate of 0.019 mg/L each hour.

(d) Use the fact from parts (a) and (c) to make a guess about C(11).  $C(11) \approx C(10) + C'(10) = 0.20 - 0.018 = 0.182 \text{ mg/L}$