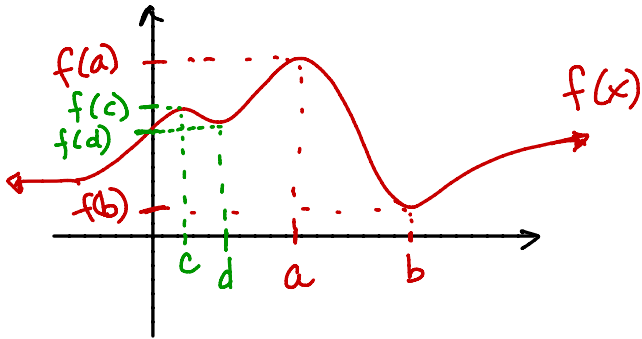


SECTION 4.3: MAXIMUMS AND MINIMUMS

- local and absolute maximums and minimums: what they are and how to find them
- critical points
- closed-interval method

1. local and absolute maximums and minimums: what they are



Note: maximums + minimums are y-values.

- $f(a)$ is an absolute maximum because $f(a) \geq f(x)$ for all x in domain
- $f(b)$ is an absolute minimum because $f(b) \leq f(x)$ for all x in domain.
- $f(c)$ is a local maximum because $f(c) \geq f(x)$ for all x in an open interval around c .
- $f(d)$ is a local minimum because $f(d) \leq f(x)$ for all x in an open interval around d .

• Critical pts

2. A variety of examples

$y = x^2$

- one absolute min. ($y=0$)
- no abs/loc max

$y = \sin(x)$

- one abs max: $y=1$
- one abs min: $y=-1$
- They occur at an infinite # of places

$y = (x+2)(x)(x-2)$

one local max, one local min

$y = |x|$

- one abs min
- no max.

$y = \frac{1}{x}$

No mins/max at all

$y = x^3$

no mins/no maxs

3. For each function below find (a) its domain, (b) any critical points, (c) use technology and the information from (b) to identify the local and/or absolute maxima and minima.

(a) $f(x) = (x - 2)^{2/3} + 1$

a. $D: (-\infty, \infty)$

b. $f'(x) = \frac{2}{3}(x-2)^{-1/3} = \frac{2}{3\sqrt[3]{x-2}}$

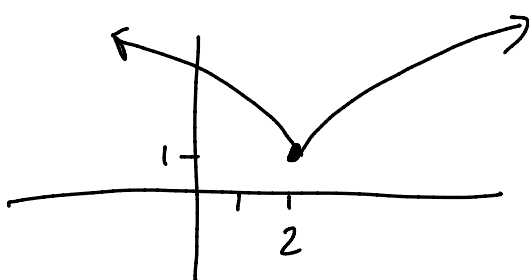
Critical number: $x=2$

f' undefined at $x=2$

$f(2) = 1$

• $f(x)$ has an absolute min of 1 at $x=2$

c.



(b) $f(x) = x^2(x - 2)^3$

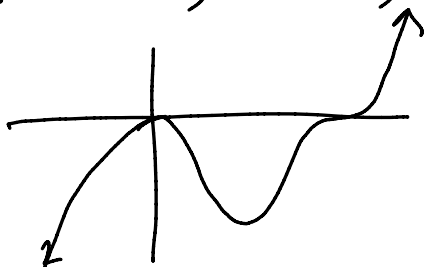
a. $D: (-\infty, \infty)$

b. $f'(x) = 2x(x-2)^3 + x^2 \cdot 3(x-2)^2$
 $= x(x-2)^2 [2(x-2) + 3x]$
 $= x(x-2)(5x-4) = 0$

Critical numbers:
 $x=0, 2, 4/5$

when $x=0, 2, 4/5$

c. $f(0)=0, f(2)=0, f(4/5)=-1.106$



• local max of 0 at $x=0$
 • local min of -1.106 at $x=4/5$