SECTION 4.7 OPTIMIZATION (DAY 1)

- 1. A Framework for Approaching Optimization
 - (a) Identify the quantity to be minimized or maximized.
 - (b) Chose notation and explain what it means.
 - (c) Write the thing you want to maximize or minimize **as a function of one variable**, including a reasonable **domain**.
 - (d) Use calculus to answer the question and *justify* that your answer is correct.

Read the problem two or three times. Draw pictures. Label them. Pick specific numerical examples, to make the problem concrete. Be creative. Try more than just one approach. Organization matters.

2. Find two positive numbers whose sum is 110 and whose product is a maximum.

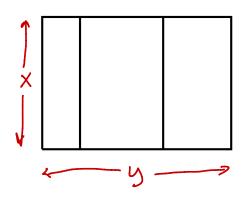
$$P(x) = x(110-x) \quad domain \quad (0, \infty)$$
$$= 110x - x^{2}$$

$$P'(x) = 1/0 - 2x$$

So Phas a local max at x=55 by the first derivative test. Since Phas only one crid. pt on (0,20), the local max is an absolute maximum.

ANS: The two numbers whose sum is 110 and whose product is a maximum are x=55 and y=55.

3. A rancher has 800 feet of fencing with which to enclose three adjacent rectangular corrals. See figure below. What dimensions should be used so that the enclosed area will be a maximum?



800 =
$$2y + 4x$$
, $y = 400 - 2x$
maximize area $A = xy$
 $A(x) = x (400 - 2x) = 400x - 2x^2$ D: $[0, 200]$
 $A'(x) = 400 - 4x$
 $A' = 0$ when $x = 100$. So $x = 100$ is the only crit.
pt of A on $[0,200]$.

Because A(x) is a parabola that opens down, A(x) must have an absolute max at x=100.

Answer: The dimensions the maximize area are x=100 ft and y=200 ft.

2