## Section 2.1: Preview of Calculuis

goals: To understand

- the difference between a secant line and a tangent line.
- how to use secant lines to estimate the slope of a tangent line.
- how to use average velocity to estimate instantaneous velocity.
- why our present tools force us to estimate slope or instantaneous velocity and not calculate it explicitly.

1. REVIEW: Write the equation of the line through the points $P(-3,1)$ and $Q(2,4)$.
2. The point $P(2,3)$ lies on the graph of $f(x)=x+\frac{2}{x}$. For each value of $x$ in the table below, find the slope of the secant line between $P(2,3)$ and $Q(x, f(x))$, if possible.

| point $Q$ |  | slope of secant line $P Q$ |
| :--- | :---: | :---: |
| $x$-value | $y$-value |  |
| $x=4$ |  | $P Q$ |
| $x=3$ |  |  |
| $x=2.5$ |  |  |
| $x=2.25$ |  |  |
| $x=2.1$ |  |  |
| $x=2$ |  |  |
| $x=1.9$ |  |  |
| $x=1.75$ |  |  |
| $x=1.5$ |  |  |
| $x=1$ |  |  |

(a) Now, use technology to sketch a rough graph $f(x)$ on the interval $(0,5]$ and add the secant lines from part $a$. (Your graph may be messy...It's ok.) Add in the tangent line to the graph at $P$. Label the secant lines with their respective slopes. What can you conclude about the slope of the tangent line to $f(x)$ at $P$ ?
(b) Write a best guess for the equation of the line tangent to $f(x)$ at point $P$. Is your equation plausible?
3. The table shows the position of a cyclist after accelerating from rest.

| $t$ (hours) | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 | 3 | 3.5 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $d$ (miles) | 0 | 9.2 | 18.7 | 23.1 | 38.1 | 46.6 | 59.7 | 72.6 | 80 |

(a) What is the cyclist's average velocity on the 4 hours of the bike ride?
(b) Estimate the cyclist's average velocity in miles per hour on each of the time intervals below:
i. $[0,1.5]$
ii. $[0.5,1.5]$
iii. $[1,1.5]$
iv. $[1.5,2]$
v. $[1.5,2.5]$
vi. $[1.5,3]$
(c) The calculations above can be used to estimate the instantaneous velocity of the cyclist at what time? What would your estimate be?

BONUS: If you understood what we did in class today, you should be able to answer the questions below.
4. In words, what is a secant line, what is a tangent line and how are they different?
5. Justify the assertion that the problem of finding the slope of the tangent to a graph at a point is the same problem as finding the instantaneous velocity of an object given its position.
6. Explain why we cannot just use our formula for slope (ie $m=\frac{\Delta y}{\Delta x}$ ) to find the slope of the tangent line?

