1. Limits at Infinity: In plain English, what should the symbols below mean?

$$\lim_{x \to \infty} f(x) = L$$
$$\lim_{x \to -\infty} f(x) = L$$

- 2. Three Principles (*a* is a constant) and a Strategy
 - If *a* is a constant, then $\lim_{x \to \pm \infty} ax =$
 - $\lim_{x \to \pm \infty} \frac{1}{x} =$
 - If $\lim_{x \to \pm \infty} f(x) = a$ and $\lim_{x \to \pm \infty} g(x) = \pm \infty$, then $\lim_{x \to \pm \infty} \frac{f(x)}{g(x)} =$
 - Strategy: Divide numerator and denominator by the highest power of *x* in the denominator.
- 3. Use the Principles to evaluate the limits below. Then, use your calculator to confirm your answer is correct.

(a)
$$\lim_{x \to \infty} \frac{2x^2 - x}{3x - 5x^2}$$

(b)
$$\lim_{x \to \infty} \frac{2x^3 - x}{3x - 5x^2}$$

(c)
$$\lim_{x \to \infty} \frac{3x + \sin(x)}{x}$$

(d)
$$\lim_{x \to -\infty} \frac{2x+1}{\sqrt{x^2+1}}$$
 (Pay attention to the sign here!)

- 4. Fill in the blanks.
 - If $\lim_{x\to\infty} f(x) = L$, then ______ is an asymptote of the graph of f(x).
 - If $\lim_{x \to -\infty} f(x) = L$, then ______ is an asymptote of the graph of f(x).
- 5. Sketch a graph of a function g(x) that satisfies all of the conditions below:
 - it's continuous on $(-\infty, \infty)$
 - it has an absolute maximum of 3 at x = 0
 - $\lim_{x \to \infty} g(x) = -5$
 - $\lim_{x \to -\infty} g(x) = 0.$
- 6. Given $f(x) = \frac{x^2}{x^2+1}$, $f'(x) = \frac{2x}{(x^2+1)^2}$, $f''(x) = \frac{-2(3x^2-1)}{(x^2+1)^3}$. Identify important features of f(x) like: domain, asymptotes, local extrema, inflection points, and make a rough sketch.