

## SECTION 4.7 OPTIMIZATION (DAY 2)

1. A rectangular container with lid is to have a volume of 36 cubic inches. The length,  $\ell$ , of the base is three times the width,  $w$ . Material for the base and lid costs \$4 per square inch. Material for the sides costs \$1 per square inch. Find the cost of materials for the least expensive container. (Recall that the volume,  $V$ , of a rectangular solid is  $V = \ell wh$ , where  $h$  is the height.)

2. Which points on the graph of  $y = 4 - x^2$  are closest to the point  $(0, 2)$ ?  
HINT: Whenever you are asked to maximize or minimize distance, it is nearly ALWAYS easier to maximize or minimize the *square* of the distance. Why?

3. Find the area of the largest rectangle that can be inscribed in a semicircle of radius  $r$ .  
**Hint:** The radius  $r$  of your circle can be considered a fixed constant. You will expect it to appear in your answer.

4. An oil refinery is located on the north bank of a straight river that is 2 km wide. A pipeline is to be constructed from the refinery to storage tanks located on the south bank of the river 10 km downstream of the refinery. The cost of laying pipe is \$ 10,000/ km over land to a point  $P$  on the opposite bank and then \$ 40,000/km under the river to the tanks. To minimize the cost of pipeline, where should  $P$  be located?