

## SECTION 5.1: APPROXIMATING AREAS

1. For all parts of this problem, the goal is to estimate the area below  $f(x) = \frac{1}{2}x^2 + 1$  and above the  $x$ -axis on the interval  $[0, 2]$ .

(a) ( $R_4$ ) Use  $n = 4$  rectangles and right-hand endpoints.

(b) ( $L_4$ ) Use  $n = 4$  rectangles and left-hand endpoints.

(c) ( $M_4$ ) Use  $n = 4$  rectangles and midpoints endpoints.

(d) Use  $R_{10}$

2. Oil leaked out of a tank at a rate of  $r(t)$  liters per hour. The rate decreased as time passed and values of the rate at 2-hour time intervals are shown in the table. Estimate how much oil leaked out. What method are you using? Is it an over estimate? Underestimate? Can you tell?

time, $t$ , (in hours)	0	2	4	6	8	10
rate, $r(t)$ , (in liters/hour)	8.7	7.6	6.8	6.2	5.7	5.3