

This quiz has two problems worth 10 points.

1. (3 points) Let $A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 1 & 3 \\ 3 & 0 & 8 \end{bmatrix}$ and $\mathbf{x} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$. Write the matrix · vector product $A\mathbf{x}$ as:

(a) a linear combination of the columns of A

(b) a single vector

(c) as dot products of rows of A

2. (7 points) Let $\mathbf{v} = \begin{bmatrix} 1 \\ 2 \\ 2 \end{bmatrix}$ and $\mathbf{w} = \begin{bmatrix} -4 \\ 1 \\ -2 \end{bmatrix}$

(a) Is the angle between \mathbf{v} and \mathbf{w} acute, right, or obtuse? Explain your answer. (Note you were not asked to find the angle.)

(b) Find a **nonzero** vector that is perpendicular to \mathbf{v} and show that you are correct.

(c) Find a **unit** vector \mathbf{u} in the same direction as vector \mathbf{v} .

(d) Find a vector \mathbf{a} such that the set of vectors \mathbf{v} , \mathbf{w} , and \mathbf{a} are **dependent**.