

This quiz is worth 10 points.

1. (2 points) Suppose  $a$  and  $b$  are  $n$ -vectors. Show that if  $a \perp b$ , then  $\|a + b\| = \sqrt{\|a\|^2 + \|b\|^2}$ .
  
  
  
  
  
  
  
  
  
  
2. (8 points) Suppose  $a = (1, 1, 0)$  and  $b = (0, 1, 1)$ .
  - (a) Is the angle between  $a$  and  $b$  acute, obtuse or a right angle?
  
  
  
  
  
  
  
  
  
  
  - (b) Write an equation for the line  $L$  between  $a$  and  $b$ . (Recall that the line determined by two points  $a$  and  $b$  is given by  $L(t) = (1 - t)a + tb$ .)
  
  
  
  
  
  
  
  
  
  
  - (c) Show that the point  $P = (3, 1, -2)$  lies on the line  $L$  determined by  $a$  and  $b$ .
  
  
  
  
  
  
  
  
  
  
  - (d) **Let  $Y$  be the point  $(7, 1, 4)$ . Show that  $P$  is the point on  $L$  that is closest to the point  $Y$ .**
  
  
  
  
  
  
  
  
  
  
  - (e) Determine the distance between  $X = (4, 0, 6)$  and  $P$ .