

This quiz is worth 10 points.

Name: _____

1. (2 points) Very briefly, explain how you can conclude *without any computation* that the vectors below are linearly **dependent**.

$$v_1 = \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}, v_2 = \begin{bmatrix} 2 \\ 1 \\ 4 \\ 3 \end{bmatrix}, v_3 = \begin{bmatrix} 1 \\ -1 \\ 1 \\ 0 \end{bmatrix}, v_4 = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \end{bmatrix}, v_5 = \begin{bmatrix} \pi \\ \sqrt{2} \\ 0 \\ 1 \end{bmatrix}$$

2. (5 points) Show the vectors $a_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix}$, $a_2 = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 0 \end{bmatrix}$, $a_3 = \begin{bmatrix} 0 \\ -1 \\ 1 \\ 1 \end{bmatrix}$ are linearly **independent**.

3. (3 points) Show that the vectors $x_1 = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$, $x_2 = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$, $x_3 = \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix}$ are linearly **dependent**.

(Note: You don't need to look too hard.)

4. (1 point bonus) Answer Question 3 above in a different way.