

## 1. Quick Review

- (a)  $R$  is an equivalence relation on  $\mathbb{R}$  defined as  $xRy$  if  $\sin(x) = \sin(y)$ . Describe and/or draw its equivalence classes.

(b) We say  $S$  is a partition of the set  $A$  if

2. Theorem 11.1: Suppose  $R$  is an equivalence relation on the set  $A$ . For every  $a, b \in A$ ,  $[a] = [b]$  if and only if  $aRb$ .

3. Theorem 11.2: Suppose  $R$  is an equivalence relation on the set  $A$ . The set  $S = \{[a] : a \in A\}$  is a partition of  $A$ .

4. Definition: The **integers modulo  $n$** , denoted  $\mathbb{Z}_n$ , is the set  $\{[0], [1], \dots, [n-1]\}$  of equivalence classes of  $\mathbb{Z}$  modulo  $n$ .

Try performing arithmetic in  $\mathbb{Z}_{10}$ . Does it depend on the representative of the equivalence class?

(a)  $[0] + [6] =$

(d)  $[3] - [7] =$

(g)  $[4] \cdot [5] =$

(b)  $[2] + [3] =$

(e)  $[6] \cdot [1] =$

(h)  $[3] \div [7] =$

(c)  $[9] + [5] =$

(f)  $[3] \cdot [7] =$

(i)  $[3] \div [4] =$

5. What do you **think** should be the definition of a relation  $R$  from the set  $A$  to the set  $B$ ?
6. Think up a relation  $R$  from  $A = \{a, b\}$  to  $B = \{1, 2, 3\}$ . How many distinct relations from  $A$  to  $B$  are possible?
7. How many relations  $R$  from  $A$  to  $B$  are functions? (This is require you to decide what you think should be the definition of a **function** from  $A$  to  $B$ ...)
8. Think up a relation  $S$  from  $C = \{a, b, c\}$  to  $D = \{1, 2, 3, 4, 5\}$  that is a function. Determine the domain and range of  $S$ .
9. In the context of relations that are functions where we already have ideas about the words **domain** and **range**, what might the term **codomain** mean?